

7.2.45 Perform the multiplication.

$$\frac{3xy - 2x^2 - y^2}{x+y} \cdot \frac{y^2 - x^2}{y^2 - 2xy}$$


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$$\frac{3xy - 2x^2 - y^2}{x+y} \cdot \frac{y^2 - x^2}{y^2 - 2xy} = \square \text{ (Type your answer in factored form.)}$$

$$3xy - 2x^2 - y^2$$

$$= -2x^2 + 3xy - y^2 \leftarrow \textcircled{A}$$

gives lead  $\neq 1$

$$\text{OR} = -y^2 + 3xy - 2x^2 \leftarrow \textcircled{B}$$

gives lead  $= 1$ .

Either  $\textcircled{A}$  or  $\textcircled{B}$  will work, but I'd choose  $\textcircled{B}$  for two reasons

- 1- It will put y-variables first, as they appear in most places in the problem
- 2- It gives lead  $= 1$  after factoring out  $-1$ .

Usually we have terms organized as

$$x^2 \quad - \quad xy \quad - \quad y^2$$

OR as

$$y^2 \quad - \quad xy \quad - \quad x^2$$

purely one variable — mixed both variables — purely the other variable

$$-y^2 + 3xy - 2x^2$$

$$= -(y^2 - 3xy + 2x^2) \quad \begin{matrix} 2 \\ -3 \end{matrix} \begin{matrix} -1 \\ -1 \end{matrix}$$

$$= -(y-2x)(y-x)$$

Problem gives:

$$\frac{-(y-2x)(y-x)}{(y-x)} \cdot \frac{(y-x)(y+x)}{y(y-2x)}$$

$$= \boxed{\frac{-(y-x)^2}{y}}$$